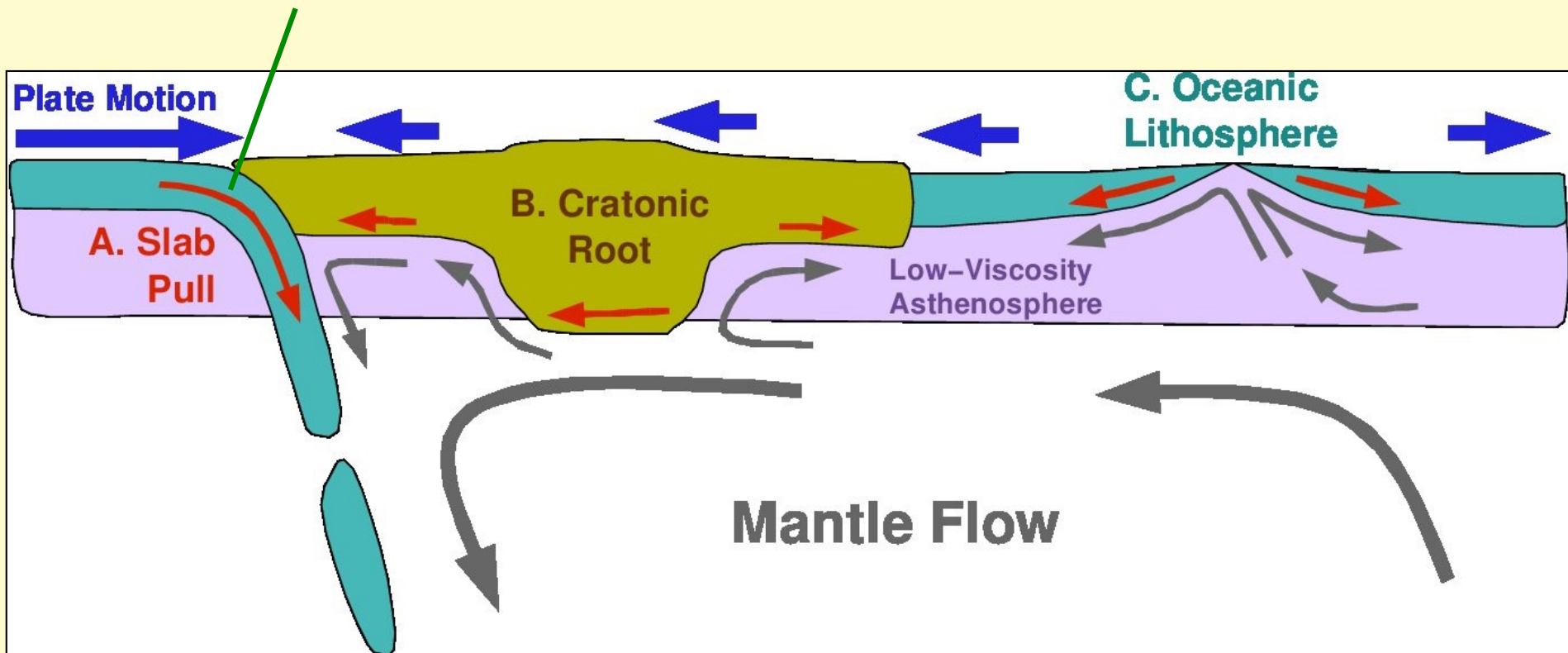


Lithosphere and Asthenosphere: Composition and Evolution

GEO-DEEP9300

Elastic Lithosphere: Valerie Maupin
Plate Flexure Clint Conrad



Geodynamic Processes of the Lithosphere & Asthenosphere

All Geodynamic Processes involve a force balance:

(Density * acceleration) =

(body force) +

(gradient of stresses) +

(material deformation)

Geodynamic Processes of the Lithosphere & Asthenosphere

All Geodynamic Processes involve a static force balance (except earthquakes):

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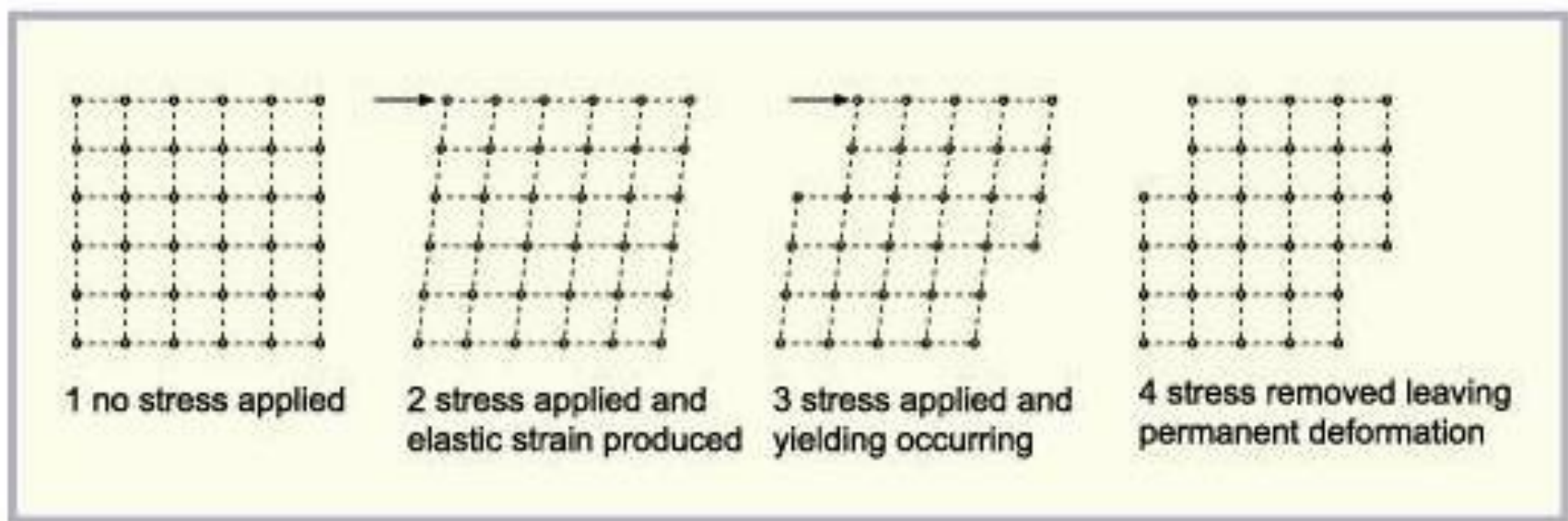
deformation depends on rheology

(material deformation)

→ **Body forces drive geodynamic processes**

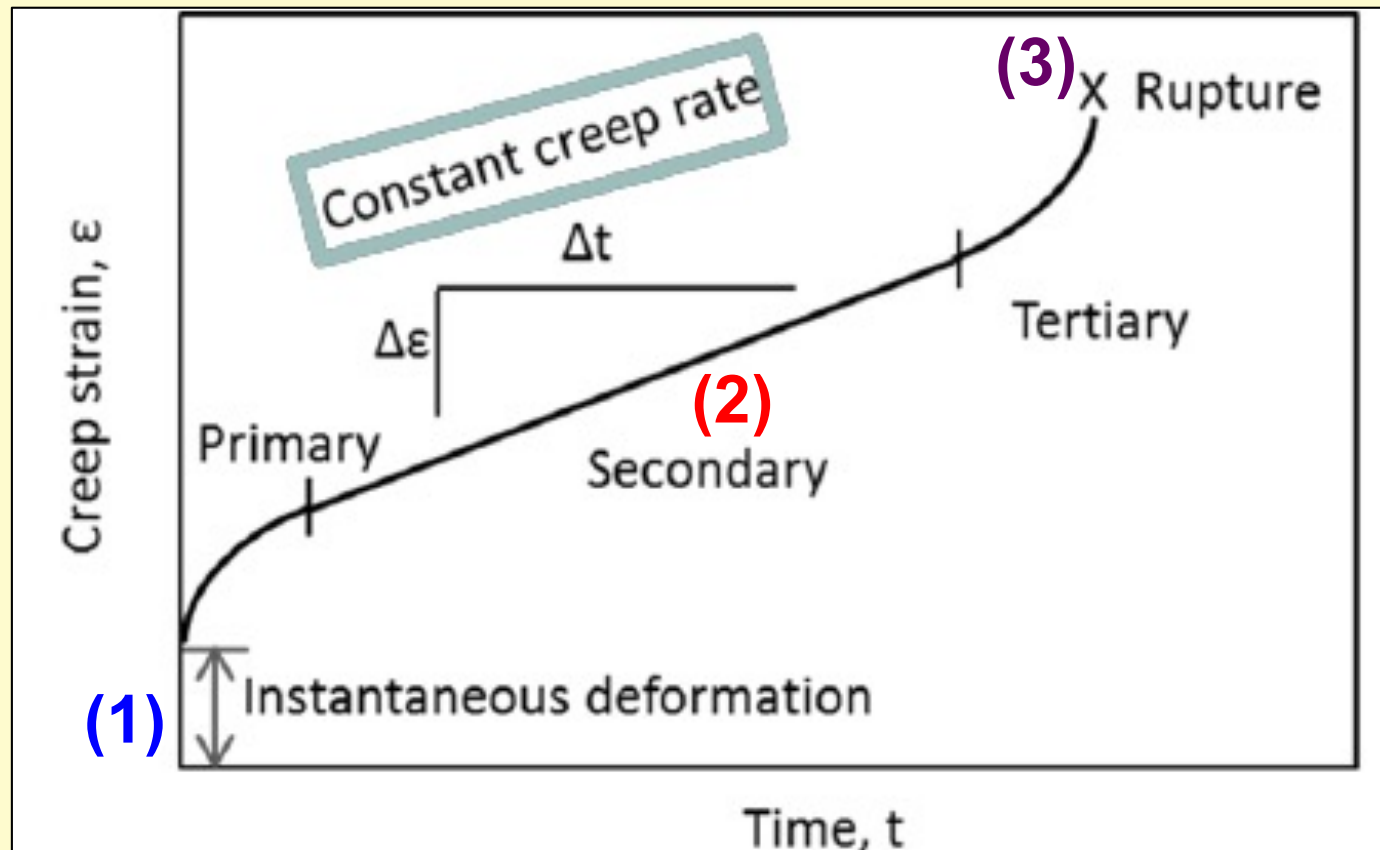
→ **Material deformation resists the body forces**

Apply a constant stress to a material: How does it deform?



Stages of Plastic Deformation

Apply a constant stress to a material: How does it deform?



Types of rheology that are important for the lithosphere:

1. Elastic Deformation: Stress \sim Strain
2. Viscous Deformation: Stress \sim Rate of Strain
3. Brittle Fracture: Strain \rightarrow infinity (discontinuity)

For a viscoelastic material:

Elastic Deformation:

$$(\text{stress}) = E (\text{strain})$$

E = Young's Modulus

$E = 70 \text{ GPa}$ (typical rock)

Viscous Deformation:

$$(\text{stress}) = \eta (\text{strain-rate})$$

η = Newtonian Viscosity

$\eta = 10^{20} \text{ Pa s}$ (typical mantle)

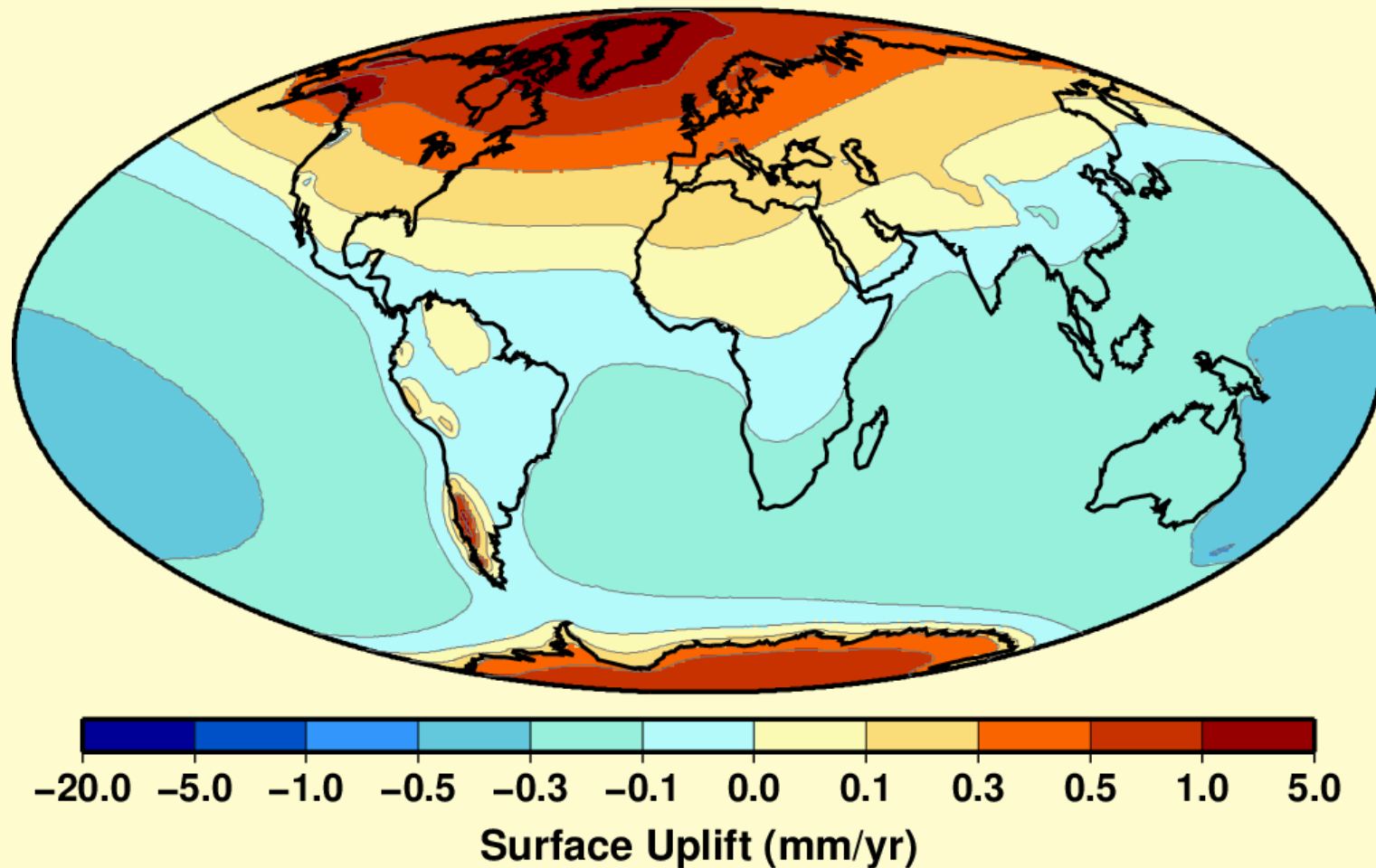
***Maxwell Time* $\sim 2\eta / E \sim 100 \text{ years}$**

The stresses relax over this timescale

**Shorter than 100 years:
Elastic deformation**

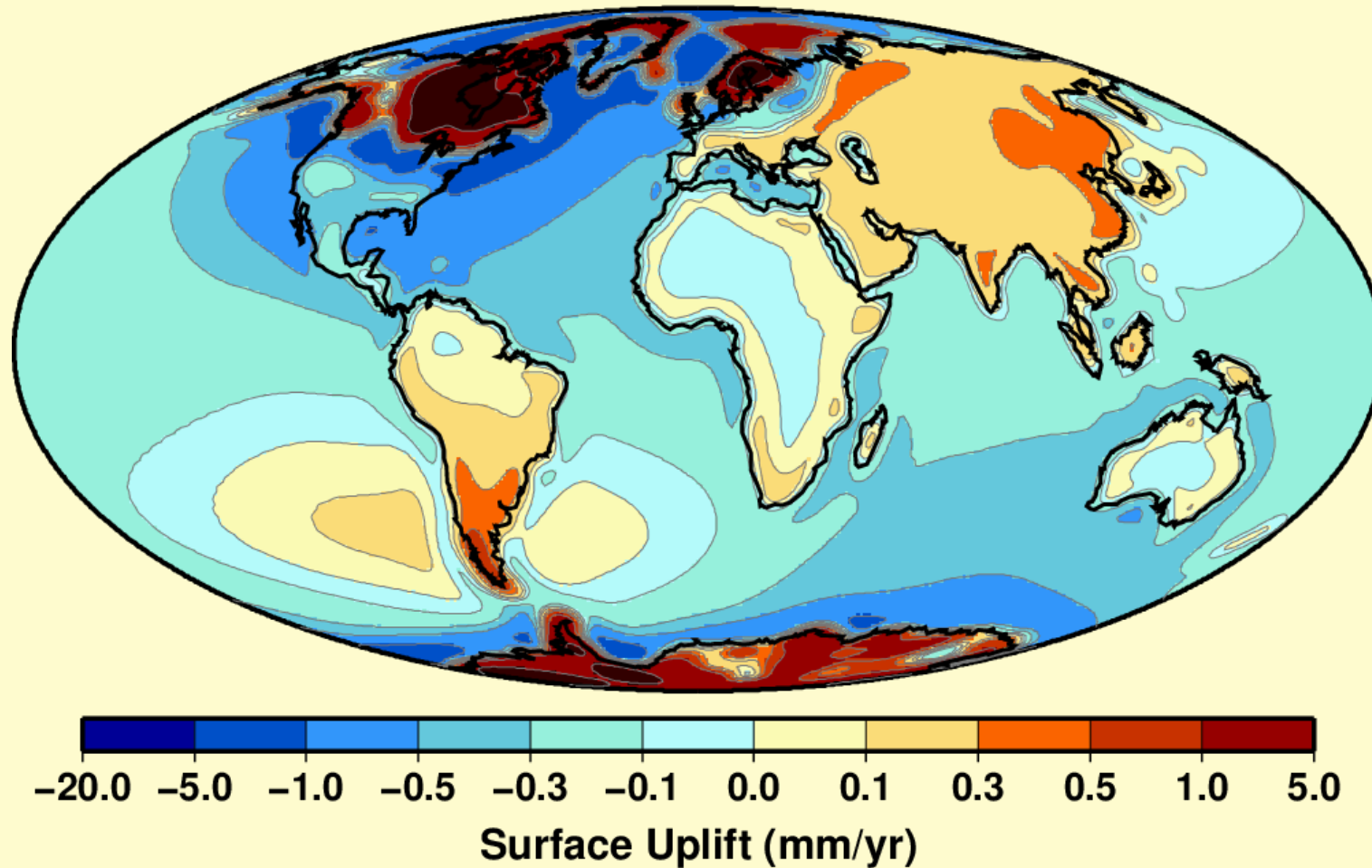
**Longer than 100 years:
Viscous deformation**

Elastic Response of the Earth to Surface Loads: Recent Ice Melt: Instantaneous Response



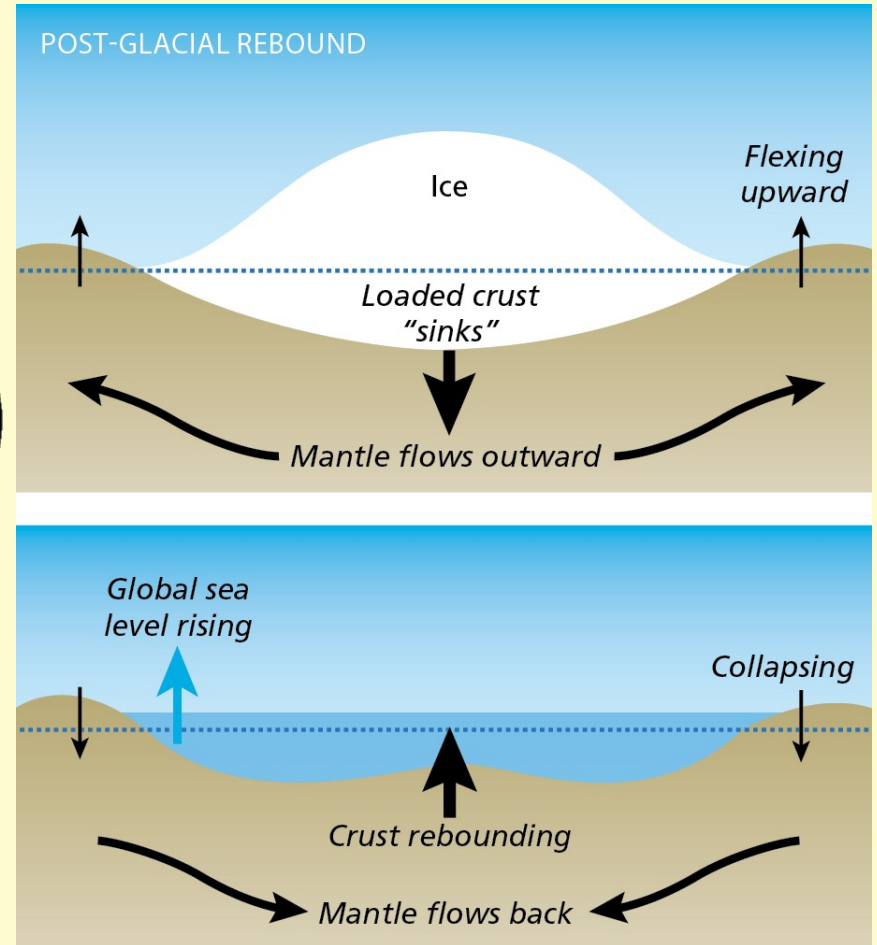
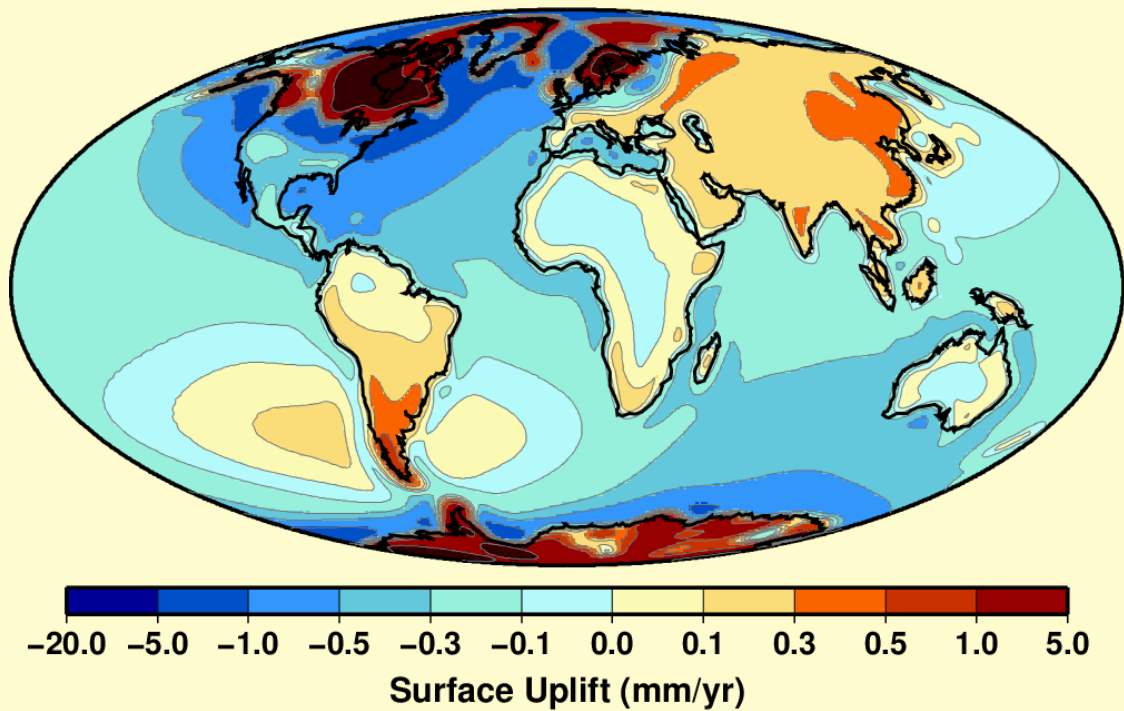
Conrad [2013]

Viscous Response of the Earth to Surface Loads: Postglacial Rebound after Last Ice Age (~10⁴ years ago)



Paulson et al. [2007]

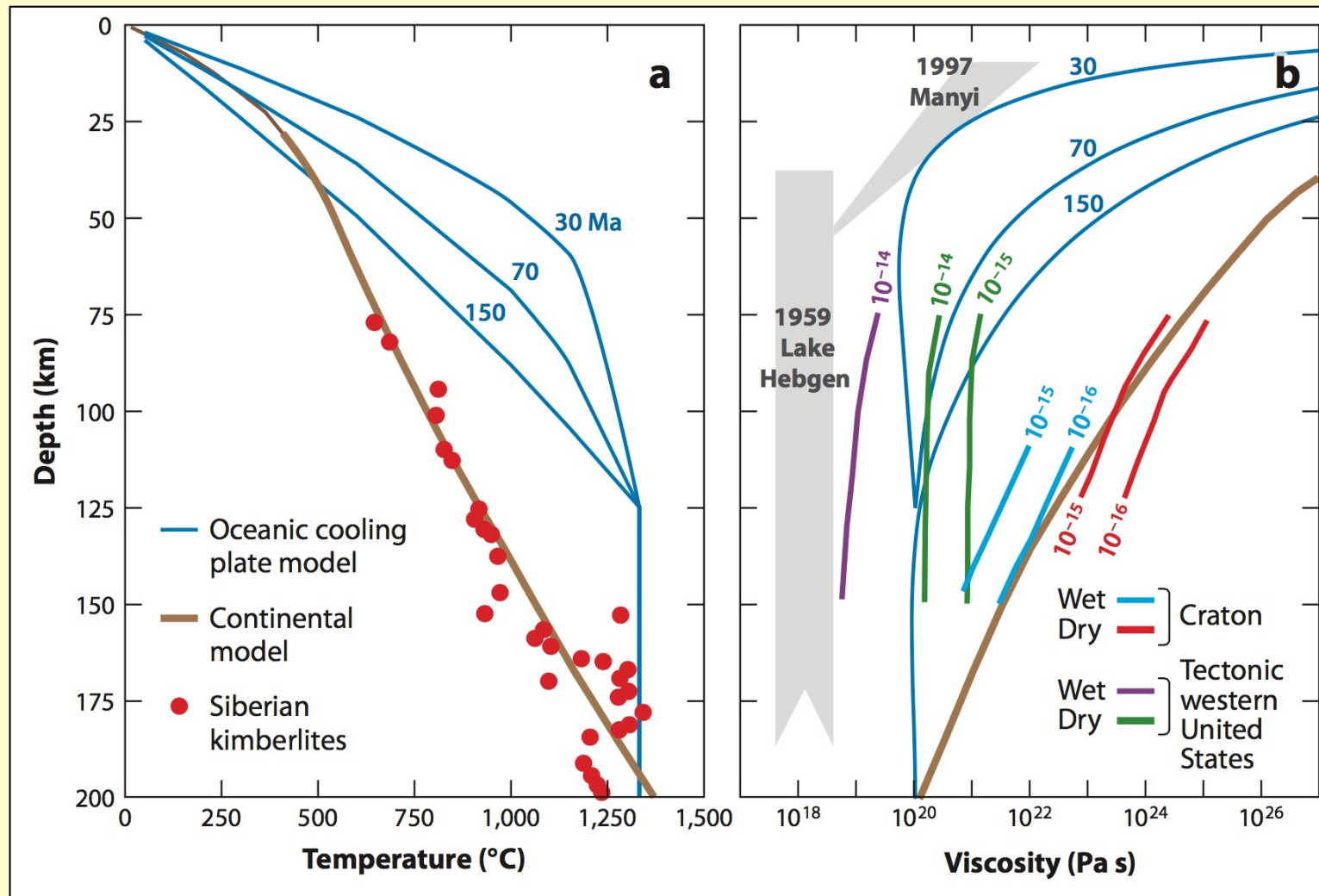
Viscous Response of the Earth to Surface Loads: Postglacial Rebound after Last Ice Age ($\sim 10^4$ years ago)



We can determine Earth's viscosity profile using postglacial rebound.

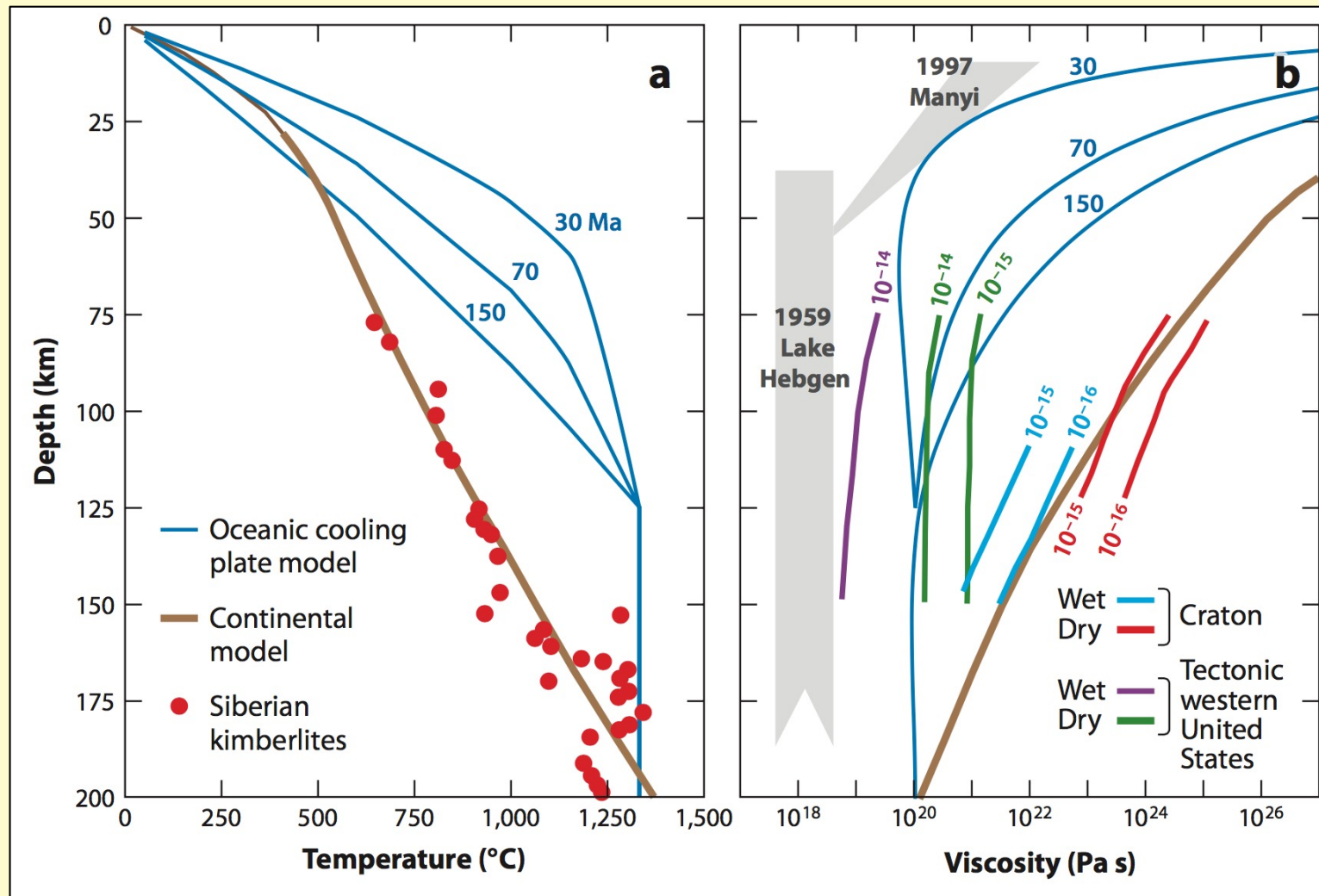
Paulson et al. [2007]

Viscosity Profile of the Lithosphere and Asthenosphere



Watts et al. [2013]

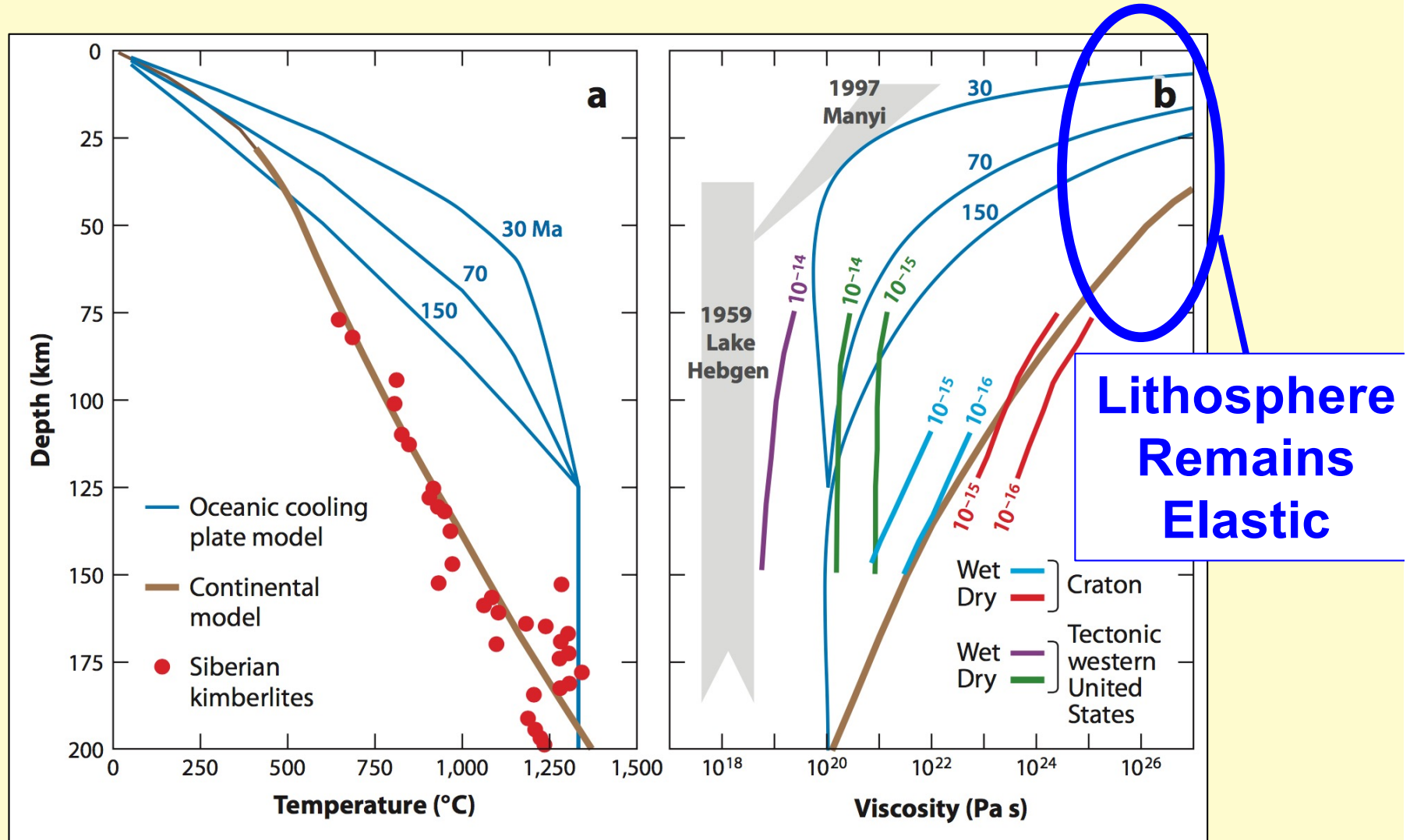
Viscosity Profile of the Lithosphere and Asthenosphere



10⁰ 10² 10⁴ 10⁶ 10⁸
 Maxwell time $\sim 2\eta / E$ (years)

Watts et al. [2013]

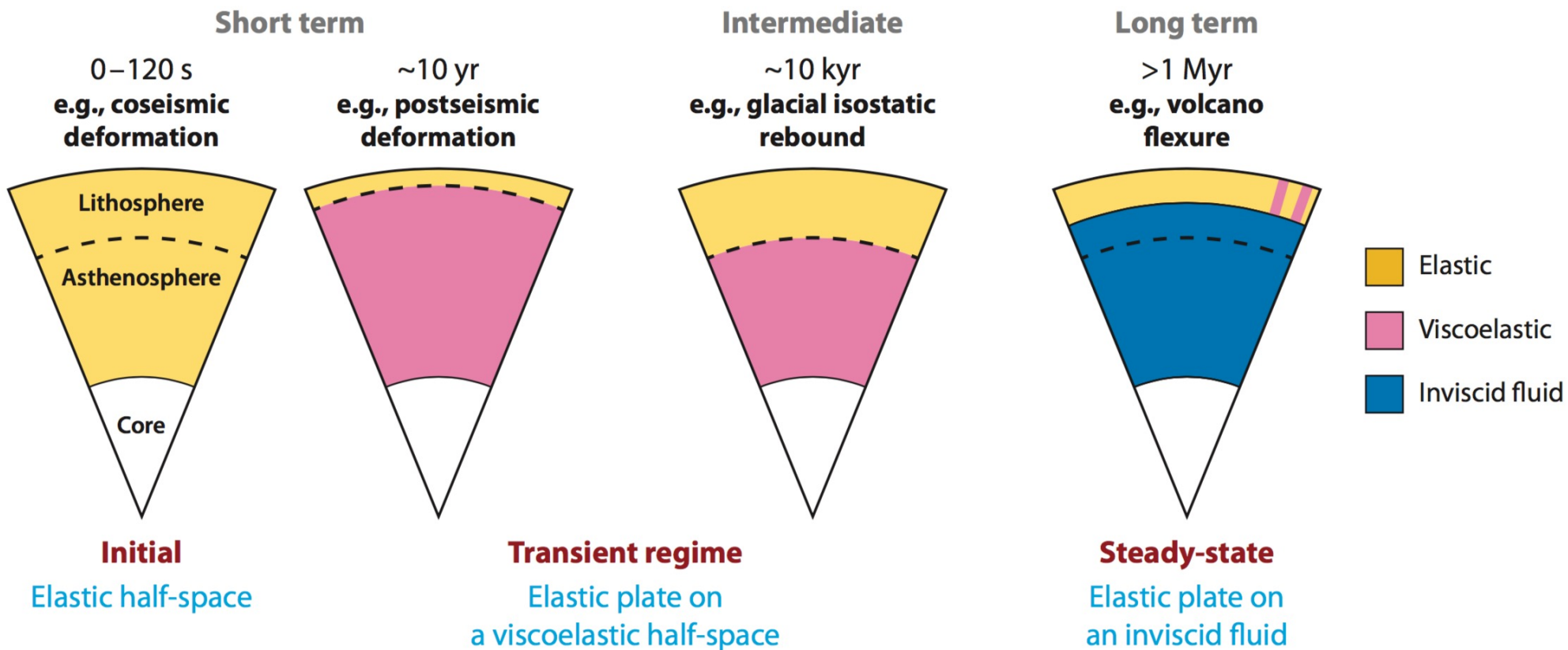
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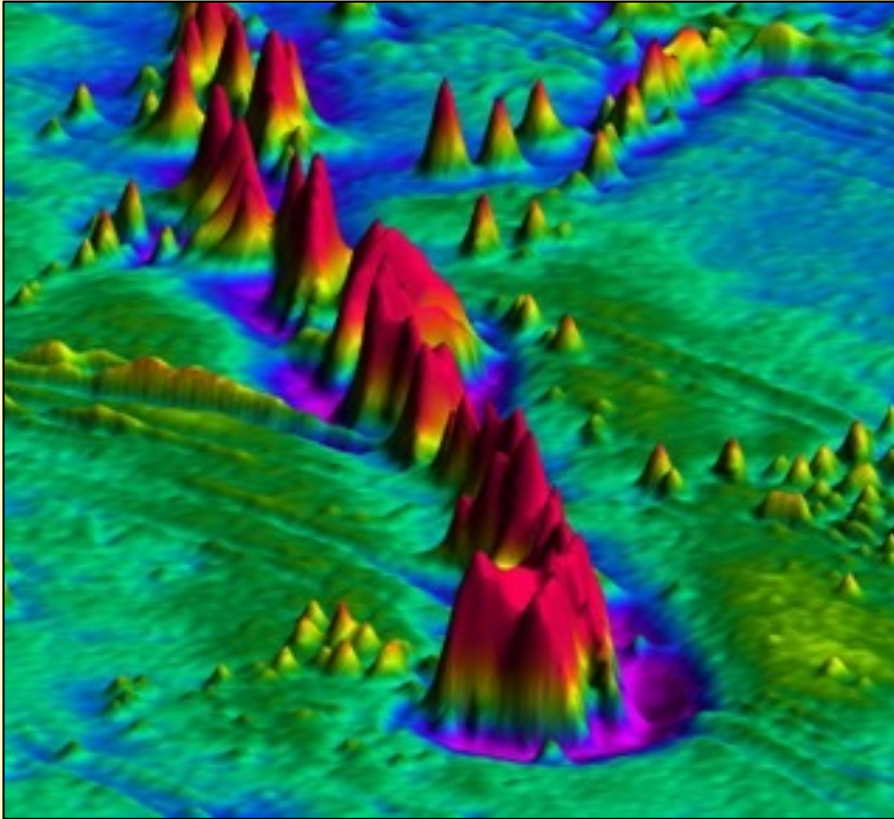
**Lithosphere
Remains
Elastic**

10⁰ 10² 10⁴ 10⁶ 10⁸
 Maxwell time $\sim 2\eta / E$ (years)

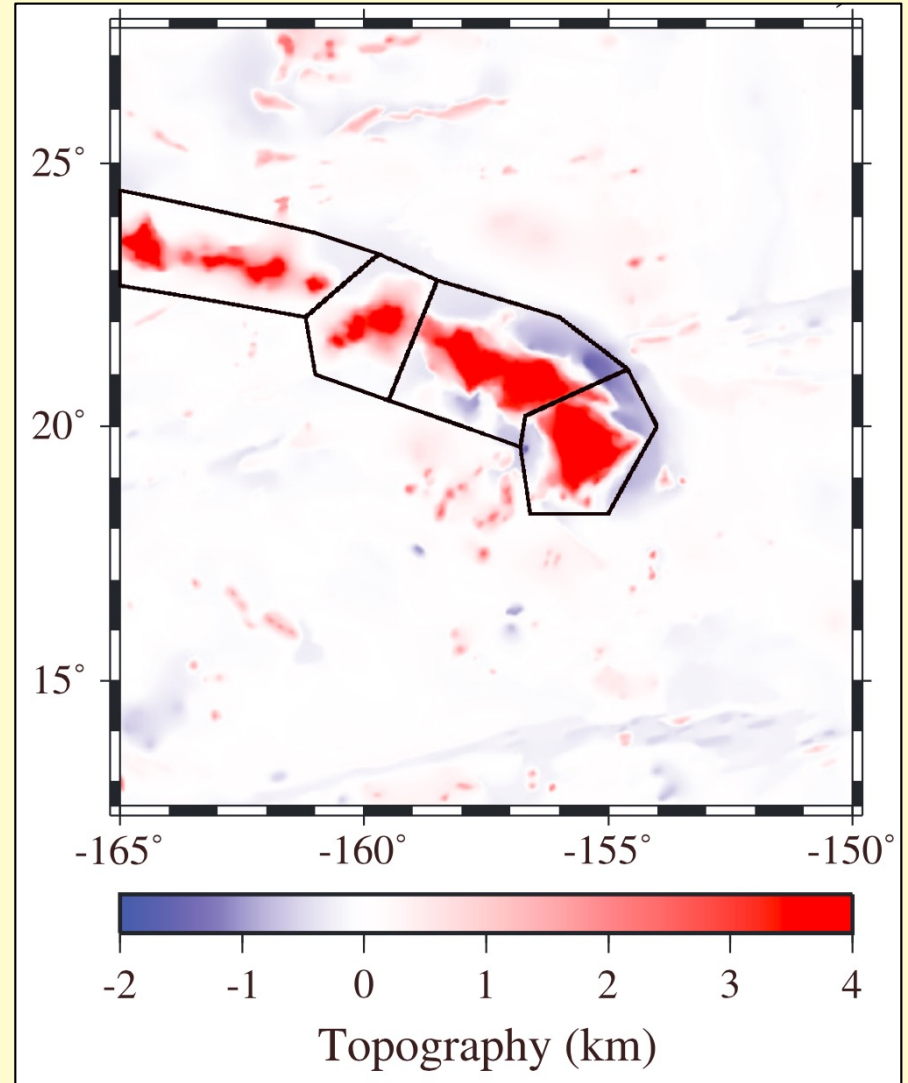
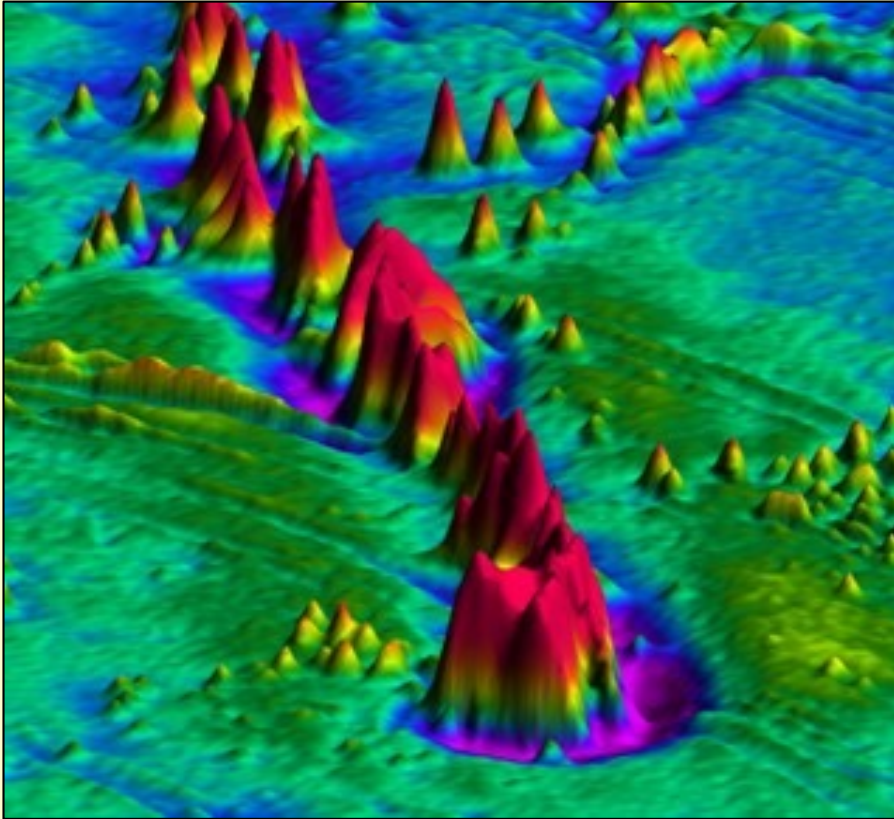
Timescale of loading determines the Earth's response: elastic vs. viscous



How does an elastic plate respond to an applied load?

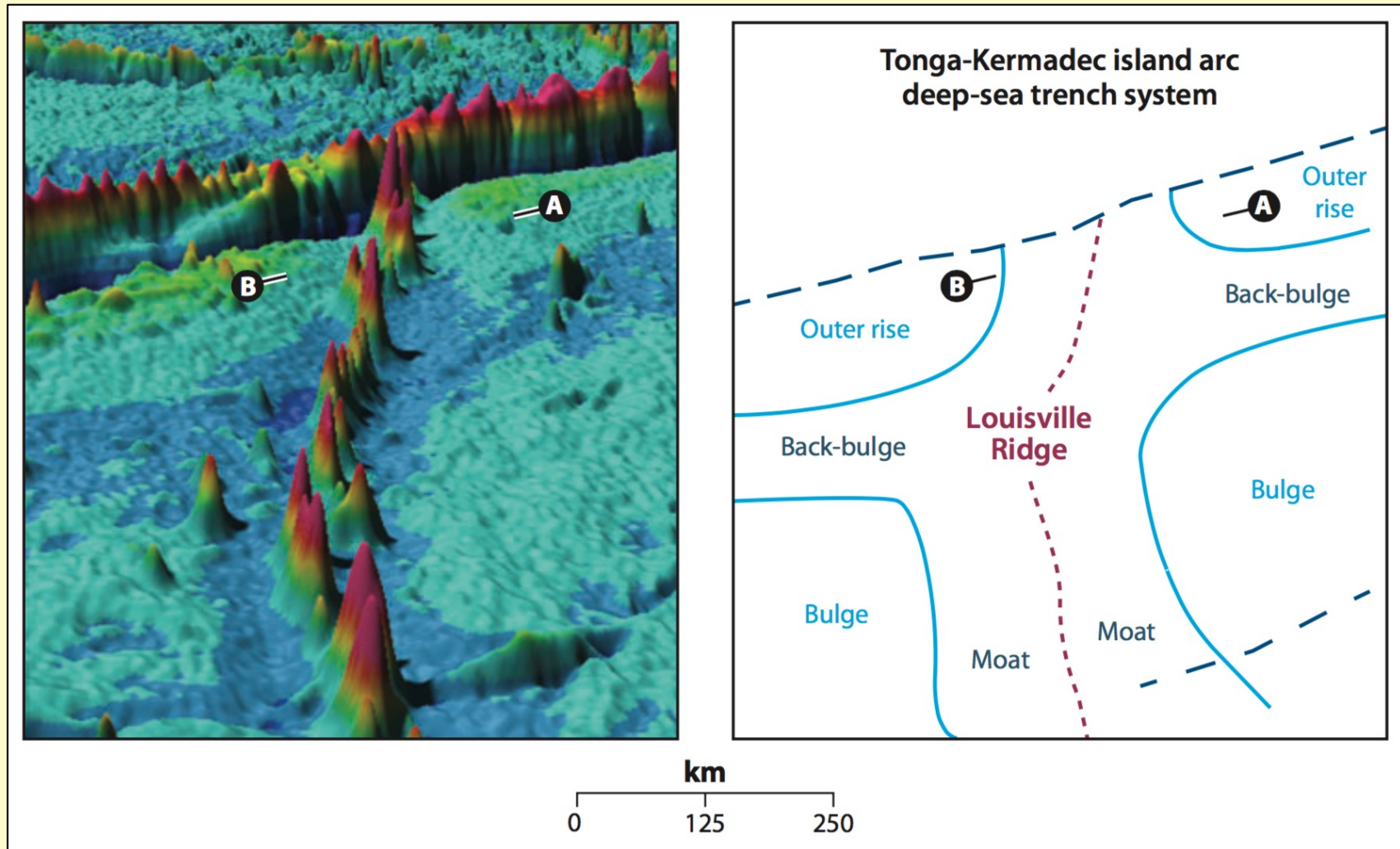


How does an elastic plate respond to an applied load?



Width of “moat” scales with the elastic thickness

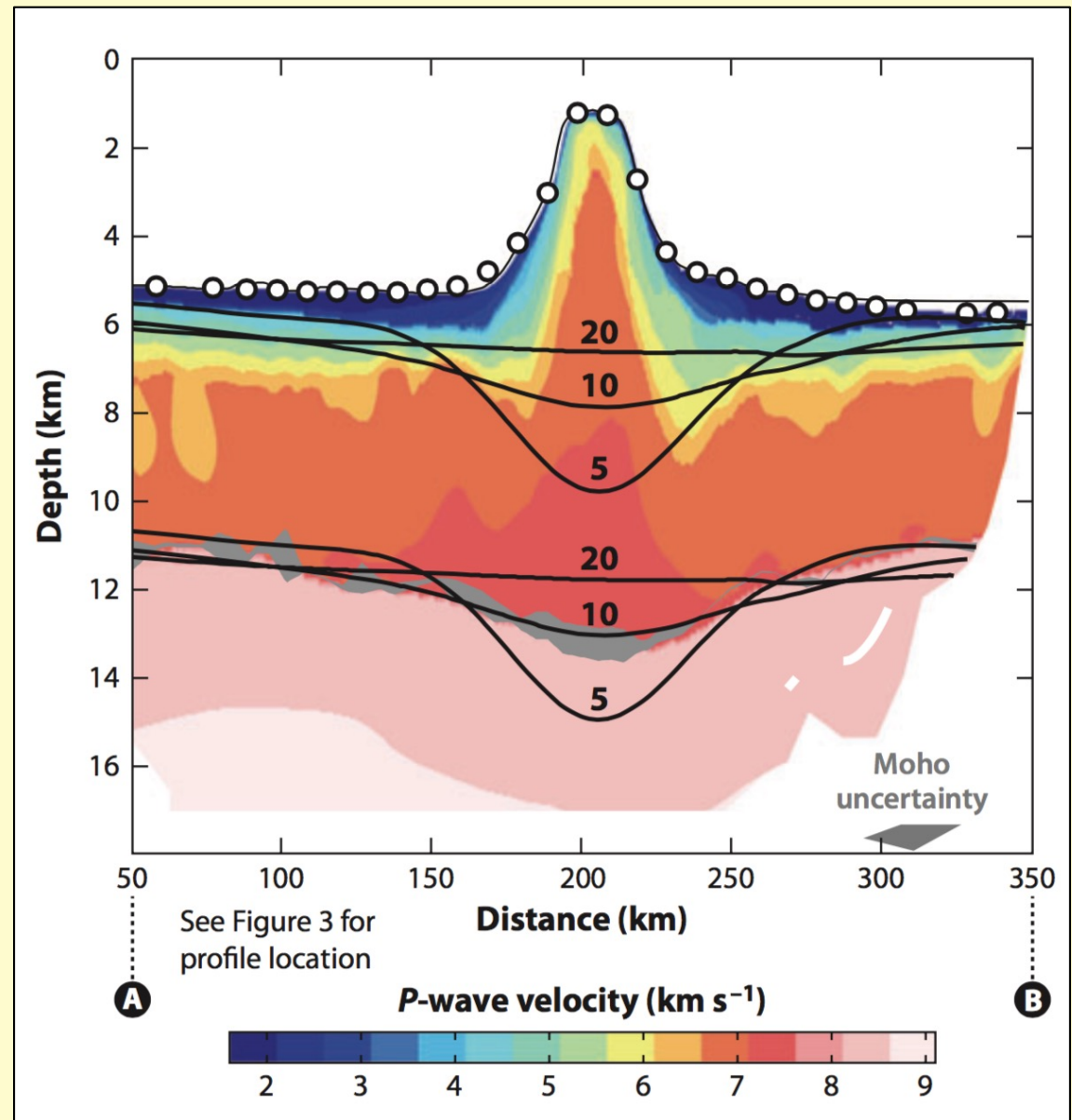
Many different volcanic loads, and subduction bending



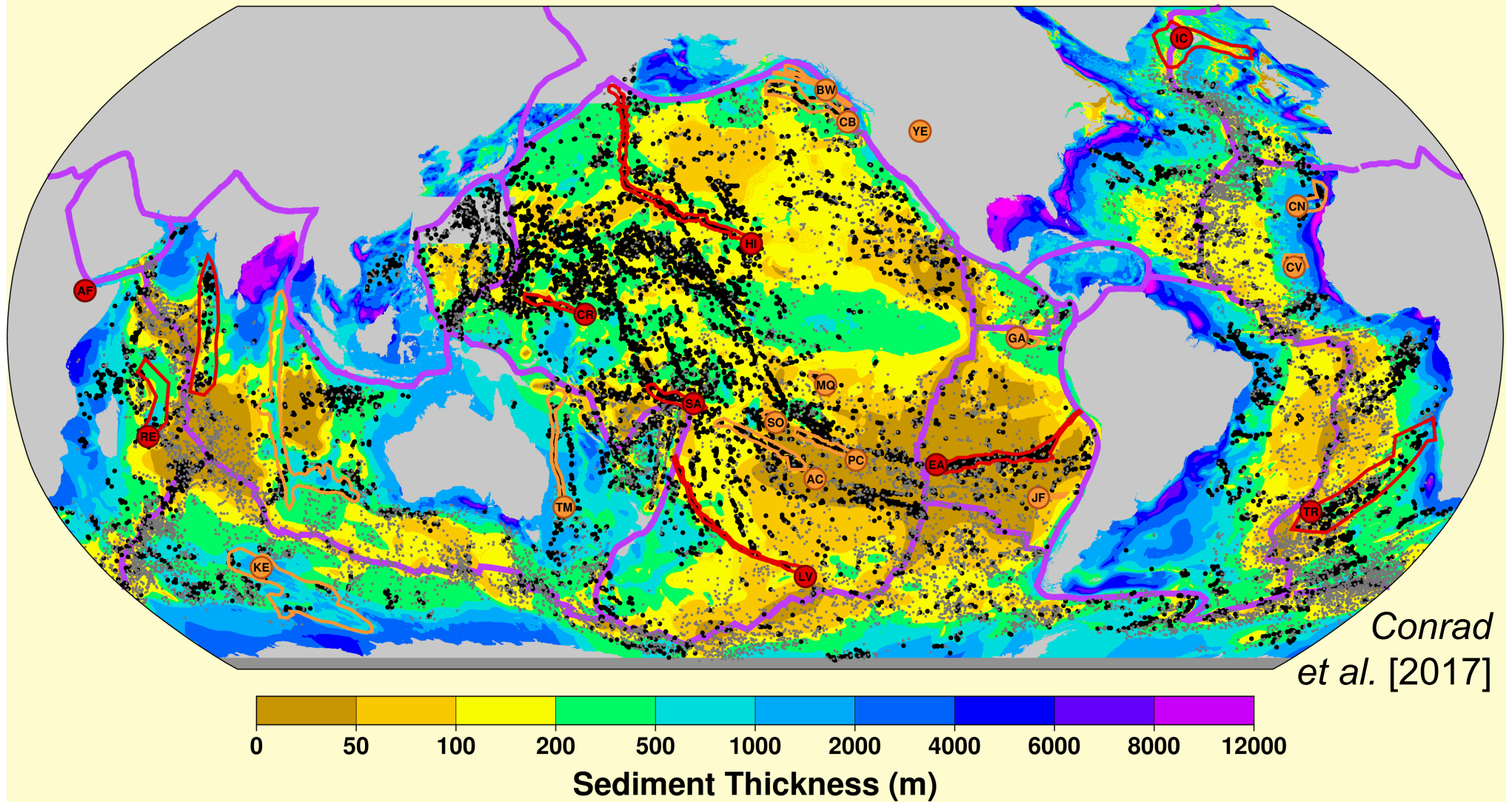
How does an elastic plate respond to an applied load?

Response of plate with different elastic thicknesses (given in km)

→ Wider deflection for thicker plate

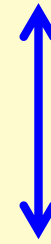
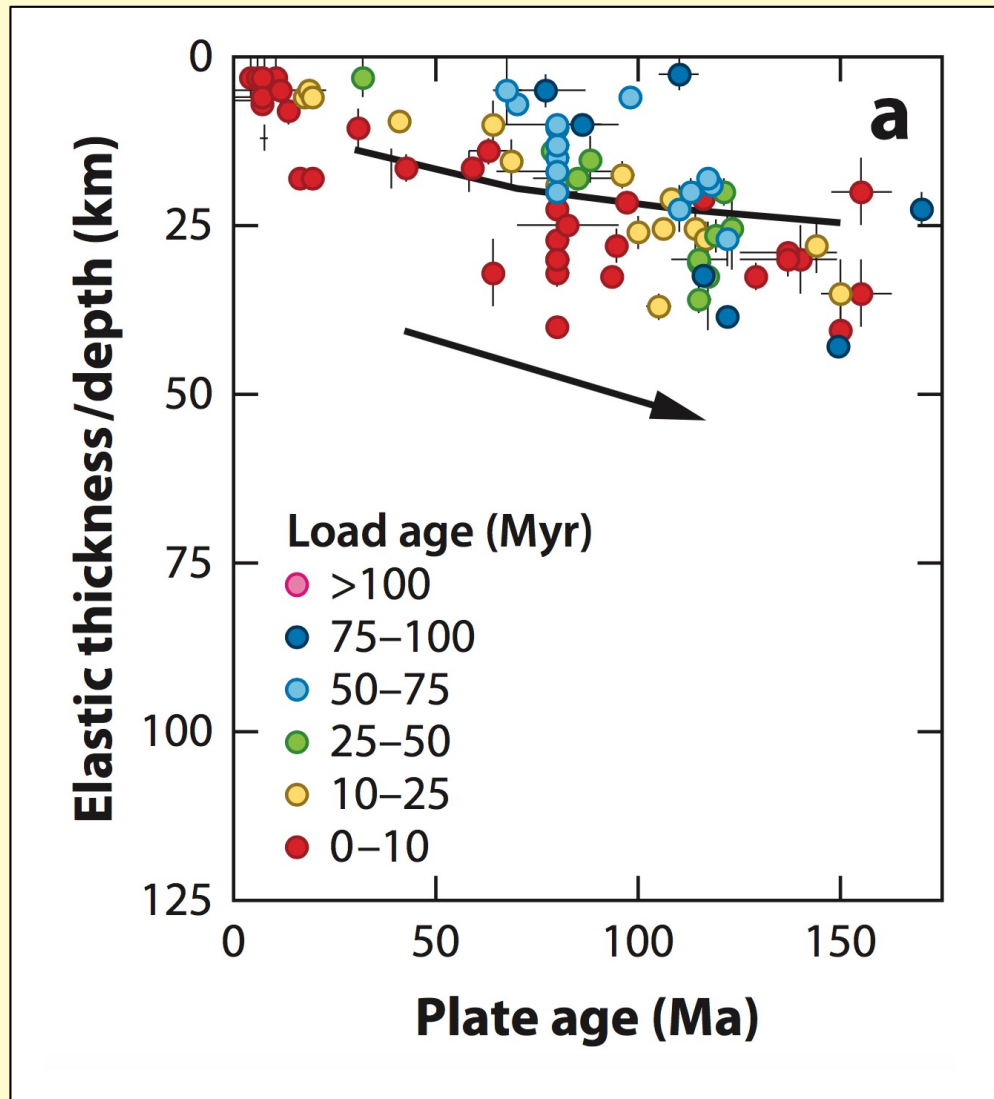


Use seamounts as loads to measure the elastic thickness



Conrad
et al. [2017]

Elastic thickness increases with plate age



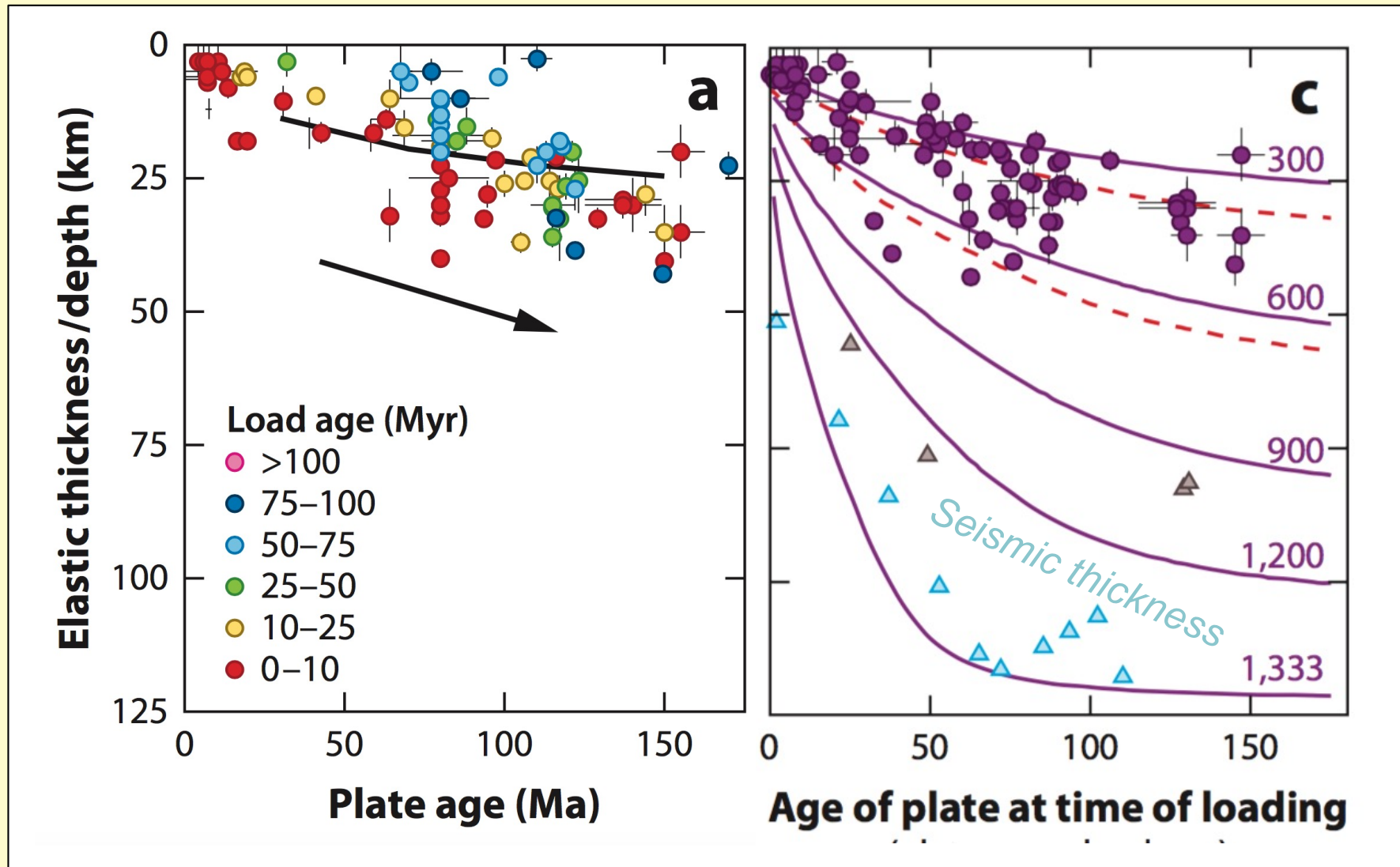
Much variation

Watts et al. [2013]

*Estimate elastic thickness from the
seafloor deflection around seamounts*

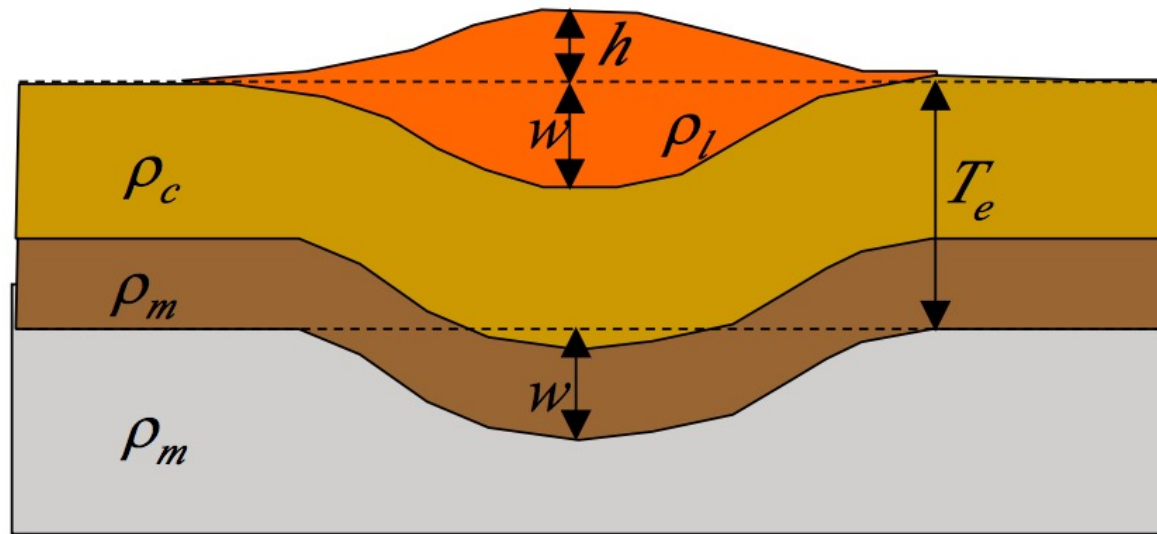
**Elastic thickness
increases with plate age**

**Elastic thickness
follows an isotherm**



Watts et al. [2013]

*Estimate elastic thickness from the
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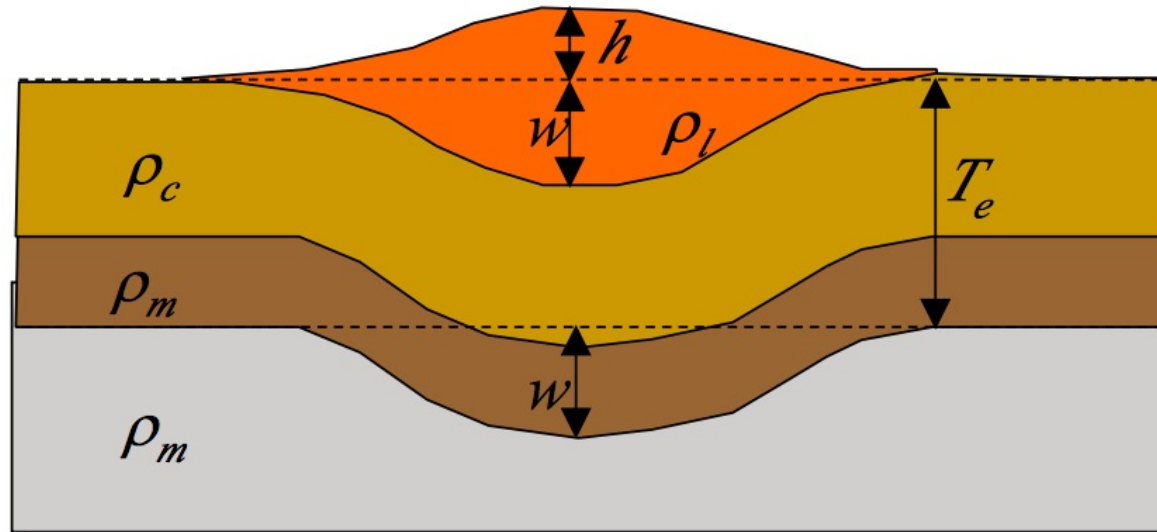


Force Balance Equation for a load on an elastic plate:

$$D \frac{d^4 w}{dx^4} + (\rho_m - \rho_l) g w = \rho_l g h$$

D is the (flexural) rigidity, T_e is the elastic thickness

$$D = \frac{ET_e^3}{12(1-\nu^2)}$$



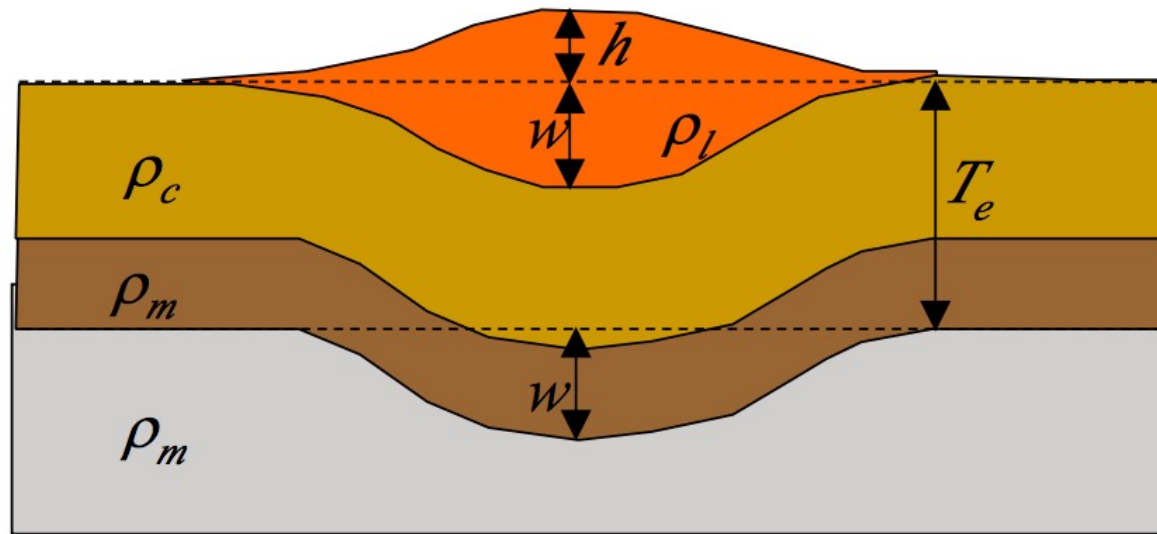
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Assume periodic solution: $w = w_0 \sin(kx)$

$$w_0 = \frac{\rho_l}{\Delta\rho + \frac{Dk^4}{g}} h_0$$

Here $\Delta\rho = \rho_m - \rho_l$ and $k = 2\pi/\lambda$, where λ is the wavelength



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Elastic flexure at short wavelengths:

$$\lambda \ll \lambda_e \rightarrow w_0 \text{ is small}$$

Elastic wavelength

$$\lambda_e \sim 400 \text{ km if } T_e = 25 \text{ km}$$

No elastic strength at long wavelengths:

$$\lambda \gg \lambda_e \rightarrow w_0 = h_0 \rho_l / \Delta\rho \text{ (isostatic compensation)}$$

Elastic Thickness of Continental Lithosphere:

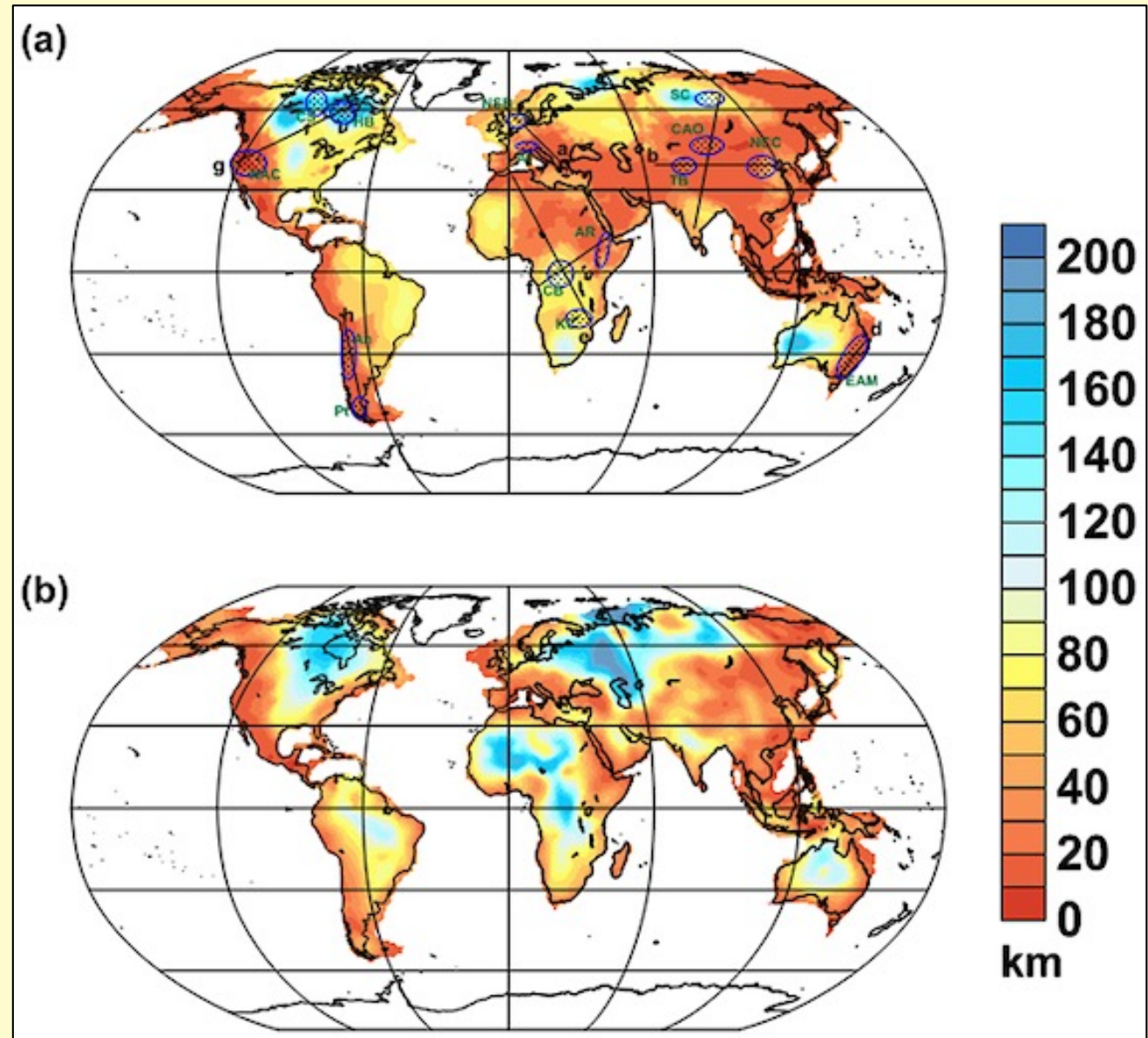
→ Strong Cratons

Based on
rheology
model

Based on
topography
to gravity
ratio

Isostatic topography
→ No gravity anomaly

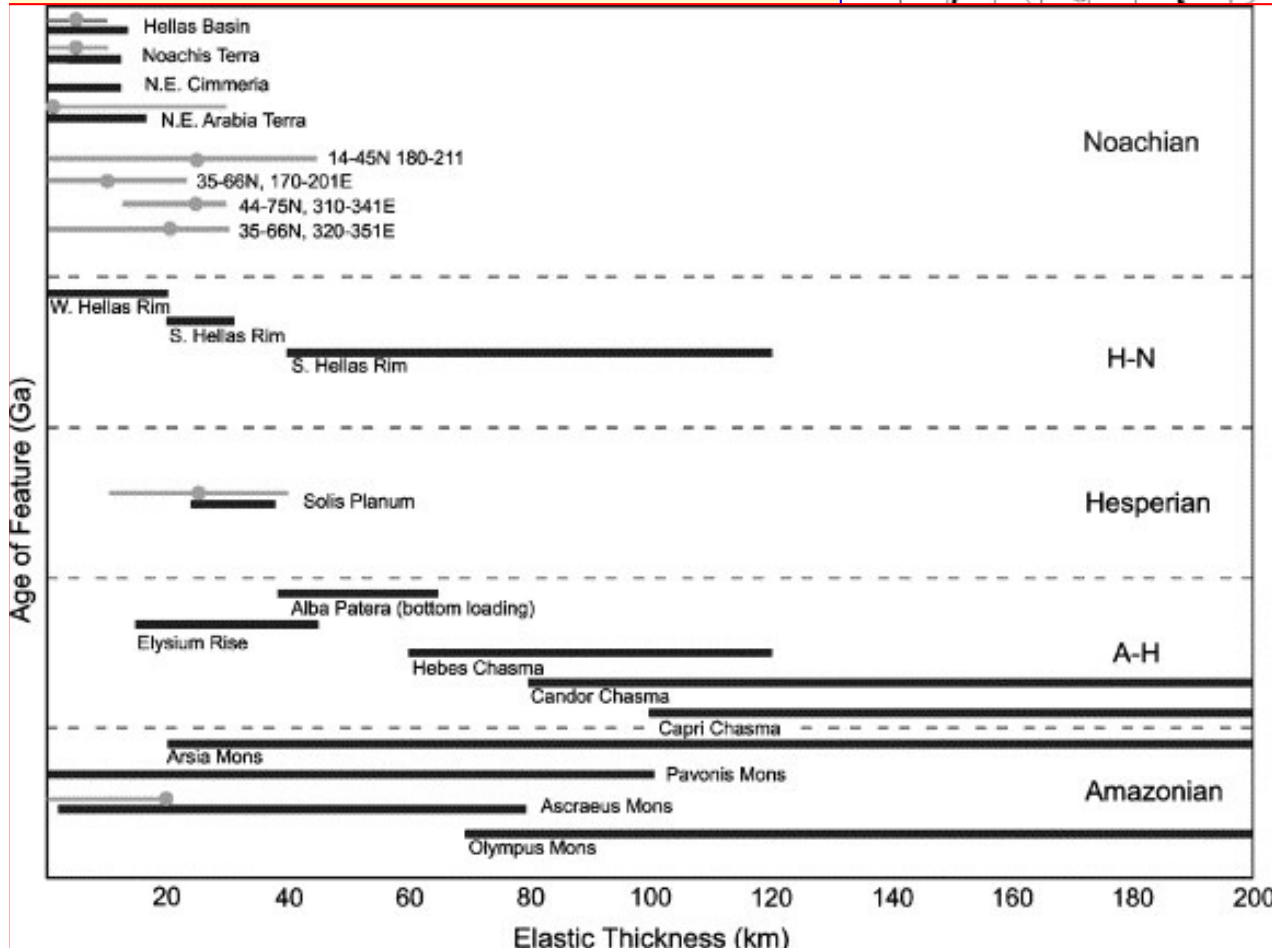
Elastic support
→ Gravity anomaly
correlates to topography



Tesauro et al. [2012]

Venus Elastic Thickness

Barnett et al. [2000]



Mars Elastic Thickness

Hoogenboom & Smrekar [2006]

Conclusions

- The top (cold) part of the lithosphere behaves elastically
- Elastic stresses can support loads up to ~ 400 km wide
- Lithosphere flexure depends on elastic thickness
- Elastic thickness depends on temperature and history

